

300-sparsians at SemEval-2018 Task 9: Hypernymy as interaction of sparse attributes

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Abstract

This paper describes 300-sparsians’s participation in SemEval-2018 Task 9: *Hypernym Discovery*, with a system based on sparse coding and a formal concept hierarchy obtained from word embeddings. Our system took first place in subtasks (1B) *Italian (all and entities)*, (1C) *Spanish entities*, and (2B) *music entities*.

1 Introduction

Natural language phenomena are extremely sparse by their nature, whereas continuous word embeddings employ dense representations of words. Turning these dense representations into a much sparser form can help in focusing on most salient parts of word representations (Faruqui et al., 2015; Berend, 2017; Subramanian et al., 2018).

Sparsity-based techniques often involve the coding of a large number of signals over the same dictionary (Rubinstein et al., 2008). Sparse, overcomplete representations have been motivated in various domains as a way to increase separability and interpretability (Olshausen and Field, 1997) and stability in the presence of noise.

Non-negativity has also been argued to be advantageous for interpretability (Faruqui et al., 2015; Fyshe et al., 2015; Arora et al., 2016). As Subramanian et al. (2018) illustrates this in the language domain, where sparse features are interpreted as lexical attributes, “to describe the city of Pittsburgh, one might talk about phenomena typical of the city, like erratic weather and large bridges. It is redundant and inefficient to list negative properties, like the absence of the Statue of Liberty”. Berend (2018) utilizes non-negative sparse coding for word translation by training

sparse word vectors for the two languages such that coding bases correspond to each other.

Here we apply sparse feature pairs to hypernym extraction. The role of an attribute pair $\langle i, j \rangle \in \phi(q) \times \phi(h)$ (where q is the query word, h is the hypernym candidate, and $\phi(w)$ is the index of a non-zero component in the sparse representations of w) is similar to *interaction terms* in regression.

Sparse representation is related to hypernymy in various natural ways. One of them is through *Formal concept Analysis (FCA)*. The idea of acquiring concept hierarchies from a text corpus with the tools of Formal concept Analysis (FCA) is relatively new (Cimiano et al., 2005). Our submissions experiment with formal concept analysis tool by Endres et al. (2010). See the next section for a description of formal concept lattices, and how hypernymys can be found in them.

Another natural formulation is related to *hierarchical sparse coding* (Zhao et al., 2009), where trees describe the order in which variables “enter the model” (i.e., take non-zero values). A node may take a non-zero value only if its ancestors also do: the dimensions that correspond to top level nodes should focus on “general” contexts that are present in most words. Yogatama et al. (2015) offer an implementation that is efficient for gigaword corpora. Exploiting the correspondence between the variable tree and the hypernym hierarchy offers itself as a natural choice.

The task (Camacho-Collados et al., 2018) evaluated systems at their ability to extract hypernyms for query words in five subtasks (three languages, English, Italian, and Spanish, and two domains, medical and music). Queries have been catego-

rized as concepts or entities. Results have been proclaimed separately in the two categories and in overall as well, thus resulting in 5×3 combinations. Our system took first place in subtasks (1B) *Italian (all and entities)*, (1C) *Spanish entities*, and (2B) *music entities*. Detailed results for our system appear in section 3. Our source code is available online¹.

1.1 Formal concept analysis

Formal Concept Analysis (FCA) is the mathematization of *concept* and conceptual hierarchy (Ganter and Wille, 2012; Endres et al., 2010). An FCA context comprises of a set of *objects* \mathcal{O} , a set of *attributes* \mathcal{A} , and a binary incidence relation $\mathcal{I} \subseteq \mathcal{O} \times \mathcal{A}$ between members of \mathcal{O} and \mathcal{A} . In our application, \mathcal{I} associates a word $w \in \mathcal{O}$ to the indices of its non-zero sparse coding coordinates $i \in \mathcal{A}$. FCA finds formal *concepts*, pairs $\langle O, A \rangle$ of object sets and attribute sets ($O \subseteq \mathcal{O}, A \subseteq \mathcal{A}$) such that A consists of the shared attributes of objects in O (and no more), and O consists of the objects in \mathcal{O} that have all the attributes in A (and no more). (There is a closure-operator related to each FCA context, for which O and A are closed sets iff $\langle O, A \rangle$ is a concept.) O is called the extent and A is the intent of the concept.

There is an order defined in the context: if $\langle A_1, B_1 \rangle$ and $\langle A_2, B_2 \rangle$ are concepts in \mathcal{C} , $\langle A_1, B_1 \rangle$ is a *subconcept* of $\langle A_2, B_2 \rangle$ if $A_1 \subseteq A_2$ which is equivalent to $B_1 \supseteq B_2$. The concept order forms a lattice. The smallest concept whose extent contains a word is said to *introduce* the object. We expect that h will be a hypernymy of q iff $n(q) \leq n(h)$ where $n(w)$ denotes the node in the concept lattice that introduces w .

The closedness of extents and intents has an important structural consequence. Adding attributes to \mathcal{A} (e.g. responses of additional neurons) will very probably grow the model. However, the original concepts will be embedded as a substructure in the larger lattice, with their ordering relationships preserved.

2 Our approach

Now we describe our system that is based on sparse non-negative word representations and FCA besides more traditional features.

We use the popular skip-gram (SG) approach (Mikolov et al., 2013) to train $d = 100$ dimensional dense distributed word representations for each sub-corpora. The word embeddings are trained over the text corpora provided by the shared task organizers with the default training parameters of `word2vec` (`w2v`), i.e. a window size of 10 and negative 25 negative samples for each positive contexts.

We derived *multi-token units* by relying on the `word2phrase` software accompanying the `w2v` toolkit. An additional source for identifying multi-token units in the training corpus was the list of potential hypernyms released for each subtask by the shared task organizers.

Given the dense embedding matrix $W_x \in \mathbb{R}^{d \times |V_x|}$, for some subcorpus of the shared task $x \in \{1A, 1B, 1C, 2A, 2B\}$, where $|V_x|$ is the size of the vocabulary and d is set to 100, as a subsequent step, we turn W_x into *sparse word vectors* akin to Berend (2017) by solving for

$$\min_{D \in \mathcal{C}, \alpha \in \mathbb{R}_{\geq 0}} \|D\alpha - W_x\|_F + \lambda \|\alpha\|_1, \quad (1)$$

where \mathcal{C} refers to the convex set of $\mathbb{R}^{d \times k}$ matrices consisting of d -dimensional column vectors with norm at most 1, and α contains the sparse coefficients for the elements of the vocabulary. The only difference compared to Berend (2017) is that here we ensure a non-negativity constraint over the elements of α .

For the elements of the vocabulary we ran the *formal concept analysis* tool of Endres et al. (2010)². In order to keep the size of the DAG outputted by the FCA algorithm manageable, we only included the query words and those hypernyms in the analysis which occur in the training dataset for the corpora. As we will see in the next section, this restriction turns out to be very useful.

Next, we determine a handful of features for a pair of expressions (q, h) consisting of a query q and its potential hypernym h . Table 1 provides an overview of the features employed for a pair (q, h) . We denote with \mathbf{q} and \mathbf{h} the 100-dimensional dense vectorial representations of q and h . Additionally, we denote with Q and H the sequence of tokens constituting the query and hypernym phrases. Finally, we refer to the set of basis vectors (in the FCA terminology, attributes)

¹https://github.com/begab/fca_hyponymy

²www.compsens.uni-tuebingen.de/pub/pages/personals/3/concepts.py

⁴At submission time, this feature did not work properly.

Core feature name	
cosine	$\frac{\mathbf{q}^T \mathbf{h}}{\ \mathbf{q}\ _2 \ \mathbf{h}\ _2}$
difference	$\ \mathbf{q} - \mathbf{h}\ _2$
normRatio	$\frac{\ \mathbf{q}\ _2}{\ \mathbf{h}\ _2}$
queryBeginsWith	$Q[0] = h$
queryEndsWith	$Q[-1] = h$
hasCommonWord	$Q \cap H \neq \emptyset$
sameFirstWord	$Q[0] = H[0]$
sameLastWord	$Q[-1] = H[-1]$
logFrequencyRatio	$\log_{10} \frac{\text{count}(q)}{\text{count}(h)}$
isFrequentHypernym ³	$c \in MF_{50}(q.type)$
sameConcept	$n(h) = n(q)$
parent	$n(q) \prec n(h)$
child	$n(h) \prec n(q)$
overlappingBasis	$\phi(q) \cap \phi(h) \neq \emptyset$
sparseDifference _{q \setminus h}	$ \phi(q) - \phi(h) $
sparseDifference _{h \setminus q}	$ \phi(h) - \phi(q) $
attributePair _{ij}	$\langle i, j \rangle \in \phi(q) \times \phi(h)$

Table 1: The features employed in our classifier. $MF_{50}(q.type)$ refers to the set of top-50 most frequent hypernyms for a given query type.

which are assigned non-zero weights in the reconstruction of the vectorial representation of q and h as $\phi(q)$ and $\phi(h)$. It is also considered as a feature whether a particular candidate hypernym h belongs to the top-50 most frequent hypernyms for the category of q (concept or entity, `isFrequentHypernym`). Modelling categories concept separately played an important role in the success of our systems.

Three additional features are defined for incorporating the concept lattice output by FCA. With $n(w)$ denoting the concept that introduces w , i.e. the most specific location within the DAG for w , our features indicate whether $n(q)$ (1) coincides with that of h , (2) is the parent (immediate successor) for that of h , or (3) is the child (immediate predecessor) for that of h . Parents, and even the inverse relation, proved to be more predictive than the conceptually motivated $q \leq h$. In Table 1, $n_1 \prec n_2$ denotes that n_1 is an immediate predecessor of n_2 . We will see in post-evaluation ablation experiments, where we refer to the above three features as the *FCA* features, that they were not useful in our submissions.

The `attributePairij`s above, our most im-

portant features, are indicator features for every possible interaction term between the sparse coefficients in α . That means that for a pair of words (q, h) we defined $\phi(q) \times \phi(h)$, i.e. candidates get assigned with the Descartes product derived from the indices of the non-zero coefficients in α . Note that this feature template induces k^2 features, with k being the number of basis vectors introduced in the dictionary matrix D according to Eq. 1.

In order to be able to rank potential candidates for previously unseen test query cases we trained a separate *logistic regression* classifier for the *concept* and *entity* types of queries relying on the `sklearn` package (Pedregosa et al., 2011)⁵ with the regularization parameter defaulting to 1.0. For each appropriate (q, h) pair of words for which h is a hypernym of q , we generated a number of *negative samples* (q, h') , such that the training data does not include h' as a valid hypernym for q . For a given query q , belonging to either of the *concept* or *entity* category, we sampled h' from those hypernyms which were included as a valid hypernym in the training data with respect to some $q' \neq q$ query phrase.

When making predictions for the hypernyms of a query, we relied on our query type sensitive logistic regression model to determine the ranking of the hypernym candidates. In our original submission we decided to treat such phrases to rank for potentially being a proper hypernym which served as a proper hypernym of at least one times on the training data for a given query type.

After the appropriate model ranked the hypernym candidates, we selected the top 15 ranked candidates and applied a *post-ranking* heuristic over them, i.e. reordered them according to their background frequency from the training corpus. Our assumption here is that more frequent words tend to refer to more general concepts and more general hypernymy relations potentially tend to be more easily detectable than more specialized ones.

3 Results

3.1 Our submissions

Our submissions were based on 200-dimensional sparse vectors computed from unit-normed 100-dimensional dense vectors with $\lambda = .3$. The sum of the two dimensions motivates our group name. For training the regression model with negative samples, 50 false hypernyms were sampled for

⁵scikit-learn.org

		without attribute pairs						with attribute pairs					
		MAP	MRR	P@1	P@3	P@5	P@15	MAP	MRR	P@1	P@3	P@5	P@15
1A	offic	8.6	18.0	13.0	8.9	8.2	7.9	8.9	19.4	14.9	9.3	8.6	8.1
1A	reprd	9.07	18.7	13.5	9.4	8.8	8.5	9.2	19.9	14.9	9.5	8.7	8.4
1B	offic	9.4	19.9	13.2	9.5	9.3	8.8	12.1	25.1	17.6	12.9	11.7	11.2
1B	reprd	9.2	19.5	12.8	8.9	8.9	8.7	12.8	26.7	18.9	13.6	12.4	11.9
1C	offic	12.5	25.9	16.6	13.6	12.6	11.5	17.9	37.6	27.8	19.7	17.1	16.3
1C	reprd	12.9	26.0	16.2	13.9	13.0	11.9	18.3	38.4	28.5	20.2	17.4	16.6
2A	offic	15.0	32.2	24.8	17.7	15.8	11.6	20.8	40.6	31.6	23.5	21.4	17.1
2A	reprd	15.1	32.4	24.4	18.0	16.2	11.8	21.5	43.7	35.6	25.3	21.8	17.0
2B	offic	19.1	36.7	27.2	23.0	20.1	15.4	29.5	46.4	33.0	31.9	28.9	27.7
2B	reprd	21.5	40.9	29.6	25.6	22.1	18.0	30.4	46.8	33.8	31.8	29.5	28.9

Table 2: Our submissions results: `offic`ial and those that can be `reprd`uced with the code in the project repo (with the `isFrequentHypernym` feature being turned off).

	MAP	MRR	P@1	P@3	P@5	P@10
1A	9.8	22.6	19.8	10.0	9.0	8.6
1A	8.8	21.4	19.8	8.9	7.8	7.5
1B	8.9	21.2	17.1	9.1	8.3	7.9
1B	7.8	19.4	17.1	8.3	6.8	6.5
1C	16.4	33.3	24.6	17.5	16.1	14.9
1C	12.2	29.8	24.6	12.0	11.3	11.0
2A	29.0	35.9	32.6	34.3	34.2	21.7
2A	28.9	35.8	32.6	34.3	34.2	21.4
2B	40.2	58.8	50.6	44.6	40.3	35.5
2B	33.3	51.5	36.2	40.1	35.8	28.4

Table 3: Baseline results, most frequent training hypernyms. We (upper) consider the most frequent hypernym in the given query type (concept or entity). For comparison, we also show the MFH baseline provided by the organizers (lower) that is based on the most frequent hypernyms in general.

each positive (q, h) training instance. One of our submissions involved attribute pairs, the other not. Both submissions used the conceptually motivated but practically harmful FCA-based features.

Table 2 shows submission results. The figures that can be reproduced with the code in the project repo (`reprd`) is slightly different from our official submissions (`offic`) for two reasons: because the implementation of `isFreqHyp` contained a bug, and because of the natural randomness in negative sampling. For reproducibility, we report result without the `isFreqHyp` feature. The randomness introduced by negative sampling is now factored out by random seeding.

	Train		Test	
1A	975(4)	0.41%	1055(4)	0.38%
1B	709(1)	0.14%	767(2)	0.26%
1C	776(2)	0.26%	625(2)	0.32%
2A	442(58)	11.60%	433(67)	13.40%
2B	366(21)	5.43%	341(17)	4.75%

(a) concept

	Train		Test	
1A	379(142)	27.26%	344(99)	22.35%
1B	249(41)	14.14%	205(26)	11.26%
1C	184(38)	17.12%	328(45)	12.06%
2A	0(0)	—	0(0)	—
2B	79(34)	30.09%	102(40)	28.17%

(b) entity

Table 4: Number of in-vocabulary (and out-of-vocabulary, OOV) queries per query types. The ratio of the latter is also shown.

3.2 Query type sensitive baselining

Our submission with attribute pairs achieved first place in categories (1B) Italian (all and entities), (1C) Spanish entities, and (2B) music entities. This is in part due to our good choice of a fallback solution in the case of OOV queries: we applied a category-sensitive baseline returning the most frequent train hypernym in the corresponding query type (concept or entity). Table 4 shows how frequently we had to rely on this fallback, and Table 3 shows the corresponding pure baseline results.

		candidate filtration off						candidate filtration on					
k	ns	MAP	MRR	P@1	P@3	P@5	P@15	MAP	MRR	P@1	P@3	P@5	P@15
200	50	6.5	14.9	13.1	7.4	6.1	5.5	12.1	25.4	18.9	12.9	11.6	10.9
200	all	6.9	15.8	14.1	7.6	6.3	5.8	13.0	27.1	19.9	14.2	12.5	11.8
300	50	6.9	15.8	13.9	7.6	6.4	5.9	12.1	25.7	19.5	13.0	11.5	11.0
300	all	8.0	17.8	15.4	8.9	7.4	6.8	13.5	28.0	21.1	14.5	12.9	12.3
1000	50	9.0	20.0	17.2	9.8	8.3	7.7	13.3	28.1	21.3	13.8	12.6	12.3
1000	all	11.6	26.1	22.5	12.5	10.8	10.0	13.6	27.2	19.4	13.9	13.2	12.8

Table 5: Post evaluation results on the 1A dataset investigating the effect of various hyperparameter choices. k and ns denotes the number of basis vectors and negative samples generated during training per each positive (q, h) pair. Best results obtained for each metric are marked as bold.

		MAP	MRR	P@1	P@3	P@5	P@15
off	off	10.3	21.3	15.0	10.6	10.1	9.6
off	on	10.1	21.1	14.9	10.5	9.9	9.5
on	off	12.1	25.4	18.9	12.9	11.6	10.9
on	on	12.1	25.3	18.7	13.0	11.6	11.0

Table 6: Ablation experiments, on the 1A dataset with $k = 200, ns = 50$ (and the implementation of `isFreqHyp` fixed). The first two columns indicate whether `attributePairij` and FCA-derived features are utilized, respectively.

3.3 Post-evaluation analysis

After the evaluation closed, we conducted ablation experiments the results of which are included in Table 6. In these experiments, we investigated the contribution of the features derived from sparse attribute pairs and FCA. These ablation experiments corroborates the importance of features derived from sparse attribute pairs and reveal that turning off FCA-based features does not hurt performance at all. For this reason – even though our official shared task submission included FCA-related features – we no longer employed them in our post-evaluation experiments.

Table 5 includes the detailed behavior of our model on subtask 1A with respect three distinct factors, that is

1. the number of basis vectors employed during sparse coding ($k \in \{200, 300, 1000\}$),
2. the number of negative training samples per positive sample ($ns \in \{50, all\}$),
3. candidate filtration being turned on/off.

The default number of negative samples (ns) generated for each positive training sample – also ap-

	MAP	MRR	P@1	P@3	P@5	P@15
1A	76.1	92.2	92.2	82.3	76.4	71.6
1B	71.2	93.4	93.4	78.5	70.9	65.7
1C	81.0	95.9	95.9	87.2	81.7	76.4
2A	72.6	89.6	89.6	81.0	75.3	64.1
2B	95.4	98.8	98.8	97.3	96.0	93.7

Table 7: Test results of an oracle system which uses candidate filtration.

plied in our official submission – is 50. In our post evaluation experiments we investigated the effects of generating more negative samples, i.e. we regarded all the valid hypernyms over the training set – not being a proper hypernym for q – as h' upon the creation of the (q, h') negative training instances. This latter strategy is referenced as $ns = all$ in Table 5.

In our official submission we regarded only those hypernyms as potential candidates to rank during test time which occurred at least once as a correct hypernym in the training data. We call this strategy as candidate filtration. Historically, we applied this restriction to speed up the FCA algorithm because this way the size of the concept lattice could be made smaller. As there are valid hypernyms on the test set which never occurred in the training data, our official submission would not be able to obtain a perfect score even in theory. Table 7 contains the best possible metrics on the test set that we could achieve as a result of candidate filtration. In our post evaluation experiments we also investigated the effects of turning this kind of filtration step off. As Table 5 illustrates, however, our scores degrade after turning candidate filtration off.

	MAP	MRR	P@1	P@3	P@10	P@15
1A	13.3	28.1	21.3	13.8	12.6	12.3
1A	19.8	36.1	29.7	21.1	19.0	18.3
1B	12.5	24.2	14.5	13.4	12.5	12.0
1B	12.1	25.1	17.6	12.9	11.7	11.2
1C	21.8	43.8	33.7	22.9	21.4	19.9
1C	20.0	28.3	21.4	20.9	21.0	19.4
2A	21.9	39.5	34.2	25.5	22.6	18.5
2A	34.0	54.6	49.2	40.1	36.8	27.1
2B	31.5	43.6	29.8	30.3	30.3	31.5
2B	41.0	60.9	48.2	44.9	41.3	38.0

Table 8: Post evaluation results for the different subtask using $k = 1000$, $ns = 50$ and hypernym candidate filtration. Upper: our system, lower: subtask winner.

Our post evaluation experiments in Table 5 suggest that it is advantageous to apply sparse representation of more expressive power (i.e. a higher number of basis vectors). Generating more negative samples also provide some additional performance boost. These previous observations hold irrespective whether candidate filtration is employed or not, however, their effects are more pronounced when hypernym candidates are not filtered.

Finally, we report our post-evaluation results for all the subtasks and compare them to the official scores of the best performing systems Table 8. It can be seen from these enhanced results for category “all” (concepts and entities mixed) that we would win (1B) Italian and (1C) Spanish. Our system would also place second in (1A) English.

4 Conclusion

In this paper we experimented with the integration of sparse word representations into the task of hypernymy discovery. We strived to utilize sparse word representations in two ways, i.e. via building concept lattices using formal concept analysis and modeling the hypernymy relation with the help of interaction terms. While our former approach for deriving formal concepts from sparse word representations was not successful, the interaction terms derived from sparse word representations proved to be highly beneficial.

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